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A Two-fold classification for composite decision about localized arm movement from EEG by SVM and QDA techniques

Anwasha Khasnobish, Saugat Bhattacharyya, Amit Konar, D.N.Tibarewala and Atulya K. Nagar

Abstract—Disabled people now expect better quality of life with the development of brain computer interfaces (BCIs) and neuroprosthetics. EEG (electroencephalograph) based BCI research for robot arm control mainly concentrates on distinguishing the left/right arm movement. But for controlling artificial arm in real life scenario with greater degrees of freedom, it is essential to classify the left/right arm movement further into different joint movements. In this paper we have classified the raw EEG signal for left and right hand movement, followed by further classification of each hand movement into elbow, finger and shoulder movements. From the two electrodes of interest, namely, C3 and C4, wavelet coefficients, power spectral density (PSD) estimates for the alpha and beta bands and their corresponding powers were selected as the features for this study. These features are further fed into the quadratic discriminant analysis (QDA), linear support vector machine (LSVM) and radial basis function kernelized support vector machine (RSVM) to classify into the intended classes. For left-right hand movement, the maximum classification accuracy of 87.50% is obtained using wavelet coefficient for RSVM classifier. For the multi-class classification, i.e., Finger-Elbow-Shoulder classification the maximum classification accuracy of 80.11% for elbow, 93.26% for finger and 81.12% for shoulder is obtained using the features obtained from power spectral density for RSVM classifier. The results presented in this paper indicates that elbow-finger-shoulder movement can be successfully classified using the given set of features.

Keywords—EEG, BCI, wavelet transformation, PSD, QDA, LSVM, RSVM

I. INTRODUCTION

Rehabilitative aids have come a long way in the last decade. Starting with mere mechanical rehabilitative aids, disabled people are now expecting better quality of life with the development of brain computer interfaces (BCIs) and neuroprosthetics [1].

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Brain computer interfaces possess immense potential to bring the disabled people back to the mainstream of life providing means of communication bypassing the conventional neuro-muscular pathways.

Thus BCI based prosthetics can help people with devastating disorders like amyotrophic lateral sclerosis, brainstem stroke, cerebral palsy, spinal cord injury etc. [2] [3]. BCI translates the electrical signals produced in the brain due to the electrical activity, that are detectable on scalp or cortical surface or within the brain, into outputs that communicate the users' intent without participation of peripheral nerves and muscles[4].

BCI output can drive a word processor, speech synthesizer, cursor, robotic arm, wheel chair etc. Healthy users might communicate via BCI when conventional interfaces are inadequate, unavailable or too demanding [5-7]. A variety of brain activities monitoring methods provide the basis for brain computer interfaces. These include invasive and non-invasive methods like electrocorticography (ECoG), functional magnetic resonance imaging (fMRI), functional near infrared spectroscopy (fNIR), magnetoencephalography (MEG) and electroencephalography (EEG). Most research seen today in the BCI field is performed with EEG of its non-invasive technology to detect different characteristic signals emitted from brain. Though EEG has inferior spatial resolution, it provides better temporal resolution.

For motor control related BCI research the rolandic mu rhythm (7-13 Hz) and central beta rhythm (above 13 Hz) originating from the sensory motor cortex are relevant [8]. During imagination or execution of body part movements, event related synchronization (ERS) in the gamma band and event related desynchronization (ERD) in the mu and beta bands of the EEG originates in our brain. Contralateral to the movement, a decrease in mu and beta rhythm occurs with the movement or preparation of movement which is referred as ERD (event related desynchronization). There occurs an increase in the power of mu and beta rhythms in the post movement phase, termed as ERS (event related synchronization) [9-14].

BCI system consists of modules to acquire brain signals, extract key features from them, and classify the features into intended classes ultimately aiming to translate into device commands. EEG based motor control study mainly relies on C3, C4 and Cz, as these lie on the scalp above the motor cortex area associated with voluntary motor control [15]. Various features like the time domain and frequency domain parameters [16-17], (STFT) [18], wavelet transforms, Spectral estimates

[19], statistical parameters [20], Hjorth parameters [21], etc. are being used. Researchers have used various intelligent algorithms [22-30] viz. back propagation neural network, multilayer perceptron, discriminant analysis, support vector machines, vector quantization etc. to classify the EEG data in intended categories.

EEG based BCI research for robot arm control mainly concentrates on distinguishing the left/right arm movement. But for controlling artificial arm in real life scenario with greater degrees of freedom, it is essential to classify the left/right arm movement further into different joint movements. In this paper we have classified the raw EEG signal for left and right hand movement, followed by further classification of each hand movement into shoulder, elbow and finger movement (Fig.1), aiming the ability of the classifiers to make composite decision. These classifications will help in the realistic development of EEG based BCI control of artificial limb.

This paper is presented in six sections. An introduction to features extraction and classification is given in section II and III respectively. Section IV describes the complete experimental and signal processing procedures employed in this study. Performance analysis of extracted features and classifiers is given in section V, followed by the conclusion in section VI.

II. FEATURE EXTRACTION

A. Wavelet transformation

Decomposing a signal into a set of basis functions are known as wavelets. These wavelets are obtained from a single prototype wavelet called the mother wavelet by dilations, contractions and shifting, which is the fundamental approach of wavelet transformation [19] [22] [31]. The mother wavelet function $\Psi_{a,b}(t)$ is given as

$$\Psi_{a,b}(t) = 1/\sqrt{a} \Psi(t-b/a) \quad (1)$$

where, $a, b \in R$, $a > 0$, and R is the wavelet space and 'a' and 'b' are the scaling factor and shifting factor respectively. The property of wavelet transformation to discriminate both temporal and spatial domain parameters make it an inevitable tool for feature extraction from EEG signals. The time frequency trade-off encountered by short time Fourier transforms (STFT) is being overcome by wavelet transformations with their multi-scale approximation allowing effective localization of the signal with various spatio-temporal characteristics. Thus for a non-stationary signal like EEG, it is an effective analysis tool. The discrete wavelet transforms analyzes the signals at different resolutions by decomposing the signal into coarse approximation and detail information. Each level includes two digital filters and two down-samplers by 2. The down-sampled outputs of the first high-pass and low-pass filters provide the detail D1 and approximation A1, respectively. The first approximation is further decomposed and the process is continued, until the desired level of decomposition is obtained. [32-33].

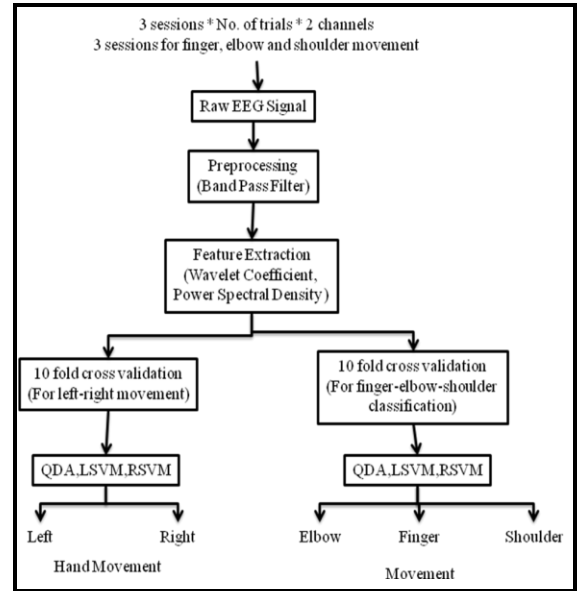


Fig.1. Proposed scheme

B. Power spectral estimates

Spectral density methods extract information from a signal to describe the distribution of its power in the frequency domain. The power spectral density (PSD) is defined as the Fourier transform (FT) of the signal's autocorrelation function, provided that the signal is stationary in a wide sense [33]. Thus for an EEG signal segmenting the complete time series data would be an ideal approach.

The measure for power spectral estimates is commonly divided into two methods; Non-parametric method and parametric method. The Welch's method fall into non-parametric method which, divides the times series data into overlapping segments, computing a modified periodogram of each segment and then the PSD estimates is averaged. Let $x_m(n) = x(n+mN)$, $n=0,1,\dots,N-1$, denote the m th block of the signal $x \in C^{MN}$, with M denoting the number of blocks. Then the Welch PSD estimate is given by [34]

$$R_x(w_k) = \sum_{m=0}^{M-1} |DFT_k(x_m)|^2 \quad (2)$$

III. CLASSIFIERS

A. Support Vector Machine

Statistical learning theory being the basis of support vector machines (SVM) provides a new approach to pattern recognition. Support vector machines (SVMs) are a set of related supervised learning methods used for classification and regression [35-36]. They belong to a family of generalized linear classifiers. SVM training always finds global minimum and its performance depends upon the selected kernel, where the user chooses only the error penalty parameter. The foundations of Support Vector Machines (SVM) have been developed by Vapnik [37] and gained popularity due to many promising features such as better empirical performance. The formulation uses the Structural Risk Minimization (SRM) principle, which has been shown

to be superior, [4], to traditional Empirical Risk Minimization (ERM) principle, used by conventional neural networks. SRM minimizes an upper bound on the expected risk, where as ERM minimizes the error on the training data. If the training data is labelled as $\{x_i, y_i\}, i = 1, \dots, l, y_i \in \{-1, 1\}, x_i \in \mathbf{R}^d$. Suppose there is some hyperplane which separates the positive from the negative examples (a “separating hyperplane”). The points \mathbf{x} which lie on the hyperplane satisfy $\mathbf{w} \cdot \mathbf{x} + b = 0$, where \mathbf{w} is normal to the hyperplane, $|b|/\|\mathbf{w}\|$ is the perpendicular distance from the hyperplane to the origin, and $\|\mathbf{w}\|$ is the Euclidean norm of \mathbf{w} . Let \mathbf{d}_+ (\mathbf{d}_-) is the shortest distance from the separating hyperplane to the closest positive (negative) example. The “margin” of a separating hyperplane is defined as $\mathbf{d}_+ + \mathbf{d}_-$. The aim of linear support vector algorithm is to find the hyperplane with largest margin. Let us assume that all the training data satisfy the following constraints:

$$\mathbf{x}_i \cdot \mathbf{w} + b \geq +1 \text{ for } y_i = +1 \quad (3)$$

$$\mathbf{x}_i \cdot \mathbf{w} + b \leq -1 \text{ for } y_i = -1 \quad (4)$$

The above two equations can be combined to obtain the following resultant:

$$y_i(\mathbf{x}_i \cdot \mathbf{w} + b) - 1 \geq 0 \quad \forall i \quad (5)$$

Considering the points for which the equality in (3) holds, these points lie on the hyperplane $H_1: \mathbf{x}_i \cdot \mathbf{w} + b = 1$, where \mathbf{w} is the normal and $|1-b|/\|\mathbf{w}\|$ is the perpendicular distance from the origin. Similarly, the points for which the equality in Eq. (11) holds lie on the hyperplane $H_2: \mathbf{x}_i \cdot \mathbf{w} + b = -1$. Hence $d_+ = d_- = 1/\|\mathbf{w}\|$ and the margin is $d_+ + d_- = 2/\|\mathbf{w}\|$.

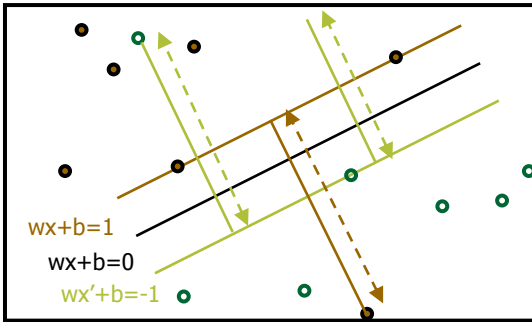


Figure 2: Representation of Hyper planes. [9]

When the vectors are separated by non-linear region, the SVM uses a kernel function to map the data into a different space where a hyperplane can be used for separating the vectors. Certain function that corresponds to an inner product in some expanded feature space is referred to as kernel function. According to Mercer’s theorem, every semi positive definite symmetric function is a kernel. Kernel function transforms the data into higher dimensional space to make it possible for the separation of the vectors (Fig. 13). The dot product becomes $K(x_i, x_j) = \varphi(x_i) \cdot \varphi(x_j)$ when every data point is mapped into high-dimensional space via some transformation $\Phi: x \rightarrow \varphi(x)$. The

kernel matrix, $K_{ij} \equiv K(x_i, x_j)$, is a Gram matrix (a matrix of dot products (Horn, 1985)) in H (i.e. the Euclidean Space) [28]. It is necessary to choose l training points such that the rank of the matrix K_{ij} increases without limit as l increases. The radial basis function is given by

$$K(x', x) = \exp \left[-\frac{\|x' - x\|^2}{\sigma^2} \right] \quad (6)$$

which defines a spherical kernel where x^t is the centre and σ , supplied by the user defines the radius.

B. Quadratic discriminant analysis(QDA)

QDA is a generalized version of linear discriminant analysis (LDA), provided there are only two classes of points and the measurements are normally distributed. However unlike LDA, the assumption that the covariance of each class is identical is not taken into consideration in QDA [38-39]. Further, the surface that separates the subspaces will be a conic section (like parabola, hyperbola, etc.). The discriminant function is given by

$$d_k(x) = 2\mu_k^T \sum_k^{-1} X - \mu_k^T \sum_k^{-1} \mu_k - 2\log \pi(k) \quad (7)$$

where, k =class, X is the set of measurements, μ_k is the mean vector, π_k is the prior probability and \sum_k is the covariance matrix.

When (7) is multiplied by -2 , the discriminant function is given by

$$d_k(x) = (X - \mu_k)^T \sum_k^{-1} (X - \mu_k) + \log |\sum_k| - 2\log \pi_k \quad (8)$$

and the discriminant rule is given by

$$d_k(X) = \min_{1 \leq k \leq K} d_k(X) \Leftrightarrow \max_{1 \leq k \leq K} p(k/x) \quad (9)$$

where, $p(k/x)$ =posterior distribution. Using this rule is called the QDA.

IV. DATA AND EXPERIMENTAL PROCEDURE

The experiment is so designed to make the subject move their left-right hand along with moving a particular portion of the hand, namely, Finger, Elbow and Shoulder in a self paced manner.

A. Subjects

Five females and three males (right handed) in the age group of 23 ± 2 years were employed as subjects in our experiment. The subjects were made to fill up a consent form and a simple introduction about the research work and stages of the experiment.

B. Visual Cue

The experiment consists of 3 sessions with 20 trials each conducted on the same day with several minutes break in between. The subjects were asked to move the right and left hand, according to the visual cue displayed on the screen. In each session, the subjects

were also asked to either move their finger, elbow or shoulder. In each trial, a blank screen was displayed in the first 2 seconds. In the 2nd second a fixation cross '+' was displayed on the screen which indicates the beginning of the trial. From the 3rd second onwards, the visual cue (left-right arrow) is displayed. At the same time, the subject was asked to move their respective limb according to the visual cue, until the display is blank again. The timing scheme of the visual cue is given below in Figure 3.

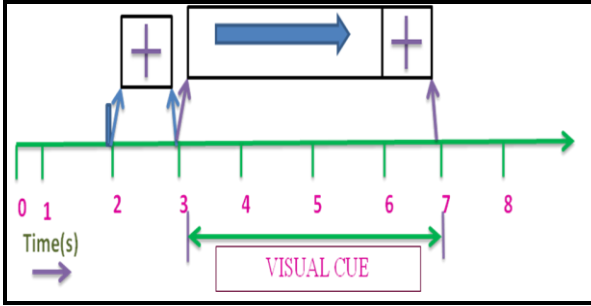


Fig.3. Timing scheme of the experiment

C. Experimental Setup

The recording of the EEG signal has been done through NeuroWin, NASAN India with 19 channel Ag/AgCl electrodes at a sampling frequency of 250 Hz and band-pass filtered between 0.01 Hz and 35 Hz. Only 3 channel electrodes; C3, Cz and C4 were selected and the electrodes are placed according to the International standard 10-20 system, the left ear was selected to be the point for the reference electrode and FPz as the ground electrode. The sensitivity of the amplifier is set to 100 μ V and an additional 50 Hz notch filter had been utilized to suppress the line noise.

D. Preprocessing

For each subject a total of 60 trials were obtained of 8 second each. Out of the three electrodes used, C3 and C4 are selected for this study as these electrodes have greater relevance for extracting information on the left-right movement. Further, the obtained data was band-pass filtered using an elliptical filter (order 14) between 8 and 30 Hz, for removing the noise based on the environment and recording techniques, and movement related information are mostly obtained in this bandwidth. The training and test data were selected randomly using the 10 fold cross validation technique which would be described later.

E. Wavelet Features Feature Extraction

In the present study, Daubechies (db) mother wavelet of order 4 is used. After trials with the EEG data, the D3 features and D4 features (Table I) i.e., the difference of the third and fourth level coefficient for the respective electrodes were selected as one of the feature components for the final feature vector (C4-C3). Figure 4 and 5 shows the D3 and D4 wavelet decomposition for left-right imagery for C3 and C4 electrode.

TABLE I
EEG SIGNAL DECOMPOSITION INTO FREQUENCY BANDS WITH A SAMPLING FREQUENCY OF 250 HZ

Frequency Range	Decomposition Level	Frequency bands
62.5-125	D1	Noise
31.25-62.5	D2	Gamma
15.625-31.25	D3	Beta
7.8125-15.625	D4	Alpha
3.91-7.8125	D5	Delta

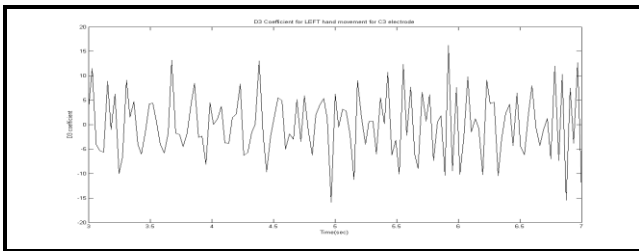


Fig.4a. Left hand movement for C3 electrode

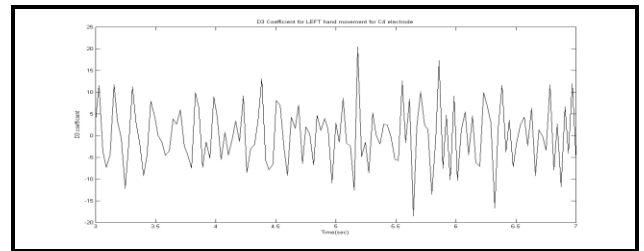


Fig.4b. Left hand movement for C4 electrode

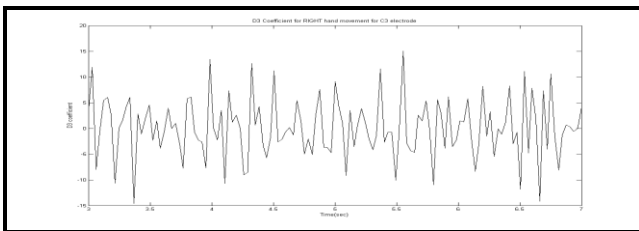


Fig.4c. Right hand movement for C3 electrode

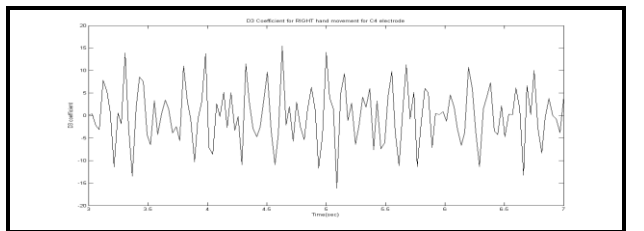


Fig.4d. Right hand movement for C4 electrode

Fig.4. D3 Coefficients for Left/Right movement for C3/C4 electrode

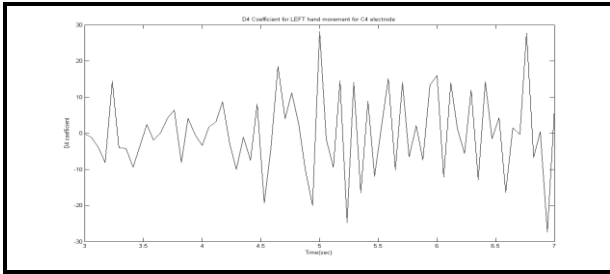


Fig.5a. Left hand movement for C3 electrode

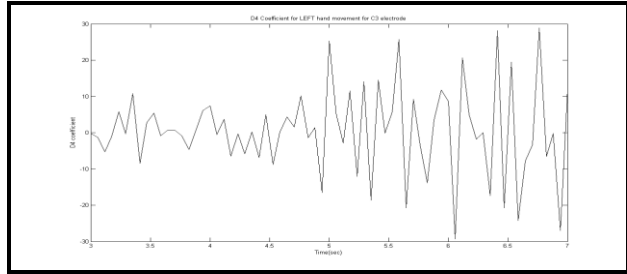


Fig.5b. Left hand movement for C4 electrode

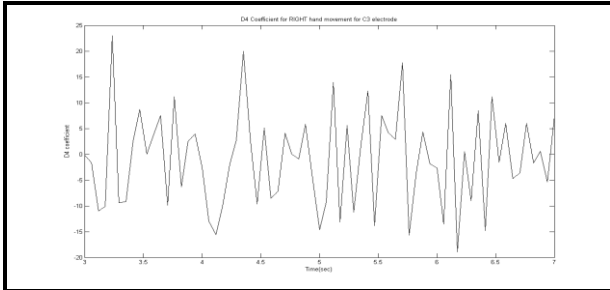


Fig.5c. Right hand movement for C3 electrode

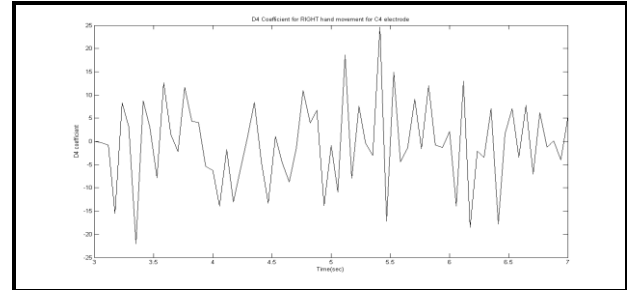


Fig. 5d. Right hand movement for C4 electrode

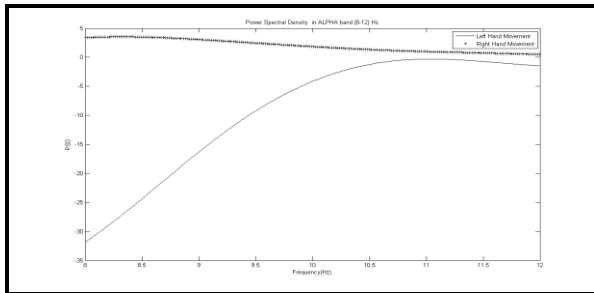
Fig.5. D4 Coefficients for Left/Right movement for C3/C4 electrode

F. Spectral Estimation Method

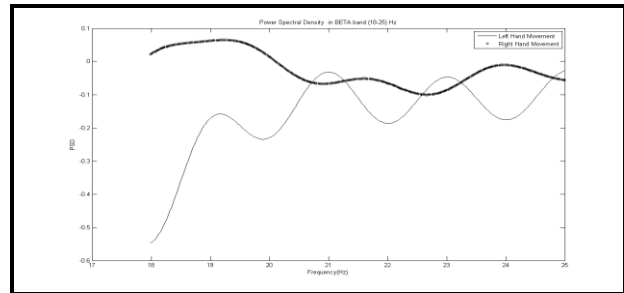
For this paper, the Welch approach was applied along with a Hamming window of length 125. The PSD estimates were obtained for the frequency band of 8-25 Hz, which comprises both the alpha or mu band (8-12Hz) and the central beta band (18-25Hz) for each respective electrode. Then the difference of the PSD estimates (1) and average power (2) is selected as another feature for this study.

$$F_{PSD} = \sum_{f=a}^b PSD_{C4}(f) - \sum_{f=a}^b PSD_{C3}(f) \quad (1)$$

where, $PSD_{C3/C4}$ is the PSD estimates of the respective electrodes in [a, b], where a & b is the frequency range (8-12Hz for alpha band and 18-25 for beta band). Figure 6 shows the power spectral density for left/right hand movement and Figure 7 and 8 shows the power spectral density for elbow/finger/shoulder movement for their respective hand.

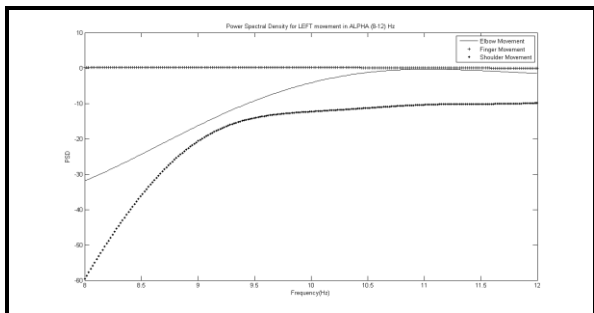


(a)

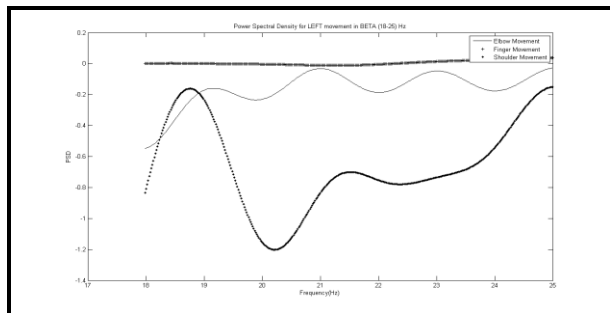


(b)

Figure 6. Power Spectral Density in (a) alpha band (b) beta band for the difference of two electrodes C3 and C4 for left/right hand movement. (- Left Movement; + Right Movement)

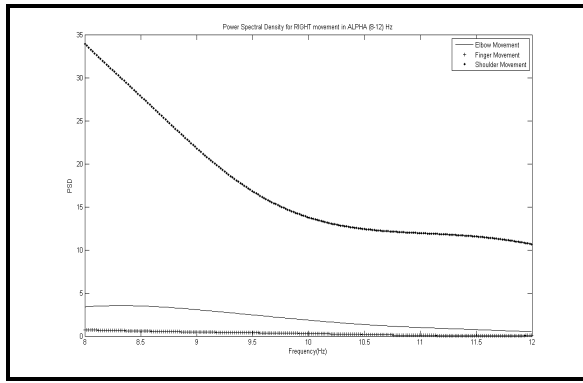


(a)

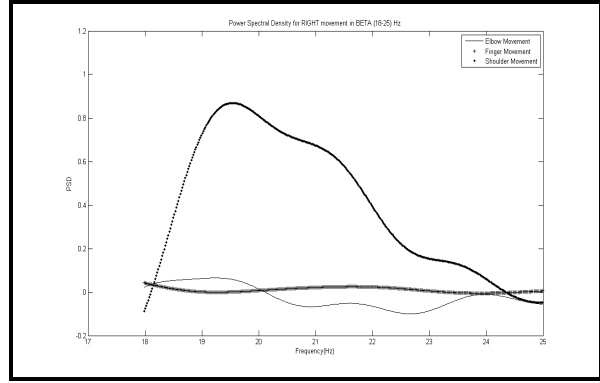


(b)

Figure 7. Power Spectral Density in (a) alpha band (b) beta band for the difference of two electrodes C3 and C4 for elbow/finger/shoulder movement for left hand. ('-' Elbow Movement; '+' Finger Movement; '.' Shoulder)



(a)



(b)

Figure 8. Power Spectral Density in (a) alpha band (b) beta band for the difference of two electrodes C3 and C4 for elbow/finger/shoulder movement for right hand. ('-' Elbow Movement; '+' Finger Movement; '.' Shoulder)

V. PERFORMANCE ANALYSIS

From the preprocessed filtered signal, only the data from the time interval $t=3$ to $7s$ are taken, marking the beginning and the end of the visual cue. From the two electrodes of interest, namely, C3 and C4, wavelet coefficients, PSD estimates for the alpha and beta bands and their corresponding powers were selected as the features for this study using the Wavelet toolbox and Signal Processing Toolbox in MATLAB. The classification ability of the obtained feature vectors can be measured through classification accuracy by averaging 10 times over a 10 fold cross validation. The 10 fold cross validation divides the number of samples into 10 disjoint sets, where 9 sets are for training and 1 set for testing. This procedure is repeated 10 times to obtain an average classification result. For our study, we have employed a two fold classification; i) left-right movement classification, and, ii) finger-elbow-shoulder movement classification. The average classification results are given in for 8 subjects using QDA and SVM (Linear and RBF-Kernel) based approaches. Since SVM is a binary class classifier, the one-against-all approach is employed for the elbow-finger-shoulder classification, i.e., for example, this approach pits the elbow movement with the rest of the movement (finger-shoulder movement) and the same for the rest of the movements. Table II and III gives the classification results for left/right hand movement for their respective features, and Table IV and V gives the classification results classification results for left/right hand movement for their respective features, and Table IV and V gives the for elbow/finger/shoulder movement for the same. For left-right hand movement, the maximum classification accuracy of 87.50% is obtained using wavelet coefficient for RSVM classifier. Also by using PSD as the feature set, the maximum classification accuracy of 87.35% is obtained for RSVM classifier.

For the multi-class classification, i.e., Finger-Elbow-Shoulder classification the maximum classification accuracy of 80.11% for elbow, 93.26% for finger and 81.12% for shoulder is obtained using the features obtained from power spectral density for RSVM classifier. While by taking the wavelet coefficient as feature set, the maximum classification accuracy of 74.24% for RSVM classifier, 72.43% for LSVM classifier

and 72.12% for RSVM classifier for elbow, finger and shoulder, respectively. In turn QDA gives an average classification accuracy, as shown in Table II, III, IV and V. All the programming was done in "offline" mode using MATLAB environment.

TABLE II
RESULT OF LEFT/RIGHT CLASSIFICATION FOR WAVELET FEATURES

Subject ID	Features	Classification Accuracy		
		QDA	LSVM	RSVM
1		.7942+/-0.0541	.8333+/-0.1700	.8615+/-0.0621
2		.6667+/-0.0786	.6092+/-0.0959	.7610+/-0.0539
3		.7667+/-0.1956	.7500+/-0.0627	.8697+/-0.0593
4	Wavelet (D3 & D4 Coeff.)	.5556+/-0.0962	.4078+/-0.1138	.5478+/-0.0315
5		.5000+/-0.2079	.6457+/-0.0589	.6392+/-0.0852
6		.8326+/-0.0222	.6449+/-0.0625	.8750+/-0.0546
7		.7500+/-0.1179	.5721+/-0.0607	.7623+/-0.0438
8		.7333+/-0.1956	.6204+/-0.0456	.7352+/-0.0500

TABLE III
RESULT OF LEFT/RIGHT CLASSIFICATION FOR PSD FEATURES

Subject	Features	Classification Accuracy		
		QDA	LSVM	RSVM
1		.7717+/-0.0567	.7774+/-0.0480	.7744+/-0.0389
2		.5075+/-0.0261	.7749+/-0.0457	.8503+/-0.0671
3		.7535+/-0.0516	.7594+/-0.1006	.8024+/-0.0747
4	PSD (Alpha & Beta Band)	.5909+/-0.0511	.6178+/-0.1512	.7147+/-0.1170
5		.6348+/-0.1255	.6851+/-0.0735	.6411+/-0.0490
6		.7745+/-0.0249	.8616+/-0.0446	.8735+/-0.0853
7		.6176+/-0.0732	.7305+/-0.0366	.7516+/-0.0543
8		.7578+/-0.0393	.6071+/-0.0444	.8047+/-0.0302

TABLE IV
RESULT OF ELBOW/FINGER/SHOULDER CLASSIFICATION FOR WAVELET FEATURES

Subject	Features	Classification Accuracy						
		QDA	LSVM-E	LSVM-F	LSVM-S	RSVM-E	RSVM-F	RSVM-S
1	Wavelet (D3 & D4 Coeff.)	.6527+/-0.0435	.5847+/-0.0484	.6112+/-0.0302	.6166+/-0.0736	.6508+/-0.0503	.6368+/-0.0548	.5753+/-0.0990
2		.4083+/-0.2306	.6714+/-0.0485	.4648+/-0.0752	.4645+/-0.0425	.6619+/-0.0596	.6383+/-0.0269	.6999+/-0.0555
3		.7017+/-0.1922	.6002+/-0.0455	.5284+/-0.0606	.5454+/-0.0865	.7424+/-0.0718	.5025+/-0.0668	.6123+/-0.0603
4		.4444+/-0.3469	.5863+/-0.0465	.5793+/-0.0381	.4384+/-0.0384	.7301+/-0.0702	.6329+/-0.0539	.6370+/-0.0948
5		.3833+/-0.2086	.4678+/-0.0396	.594+/-0.0676	.5079+/-0.0656	.6864+/-0.0272	.5923+/-0.0884	.7212+/-0.0914
6		.6080+/-0.1041	.5298+/-0.0315	.7243+/-0.0282	.7086+/-0.0551	.6044+/-0.0985	.6936+/-0.1138	.6833+/-0.0157
7		.7300+/-0.2236	.6937+/-0.1166	.5773+/-0.0543	.6229+/-0.0512	.6891+/-0.0628	.5968+/-0.0363	.6704+/-0.0344
8		.6900+/-0.2049	.5157+/-0.0678	.6823+/-0.0328	.5420+/-0.0295	.6863+/-0.0430	.6137+/-0.0529	.6272+/-0.0633

'-e'-elbow classification; '-f' -finger classification; '-s'- shoulder classification

TABLE V
RESULT OF ELBOW/FINGER/SHOULDER CLASSIFICATION FOR PSD FEATURES

Subject	Features	Classification Accuracy						
		QDA	LSVM-E	LSVM-F	LSVM-S	RSVM-E	RSVM-F	RSVM-s
1	PSD (Alpha & Beta band)	.5919+/-0.0603	.6505+/-0.0268	.6820+/-0.0741	.6470+/-0.0573	.6237+/-0.0568	.6701+/-0.0626	.6913+/-0.0582
2		.4644+/-0.0652	.8509+/-0.0963	.9093+/-0.0780	.6807+/-0.0330	.7574+/-0.0490	.9326+/-0.0307	.8112+/-0.0679
3		.6355+/-0.0859	.6868+/-0.0348	.6311+/-0.0886	.6101+/-0.0498	.6560+/-0.0747	.5682+/-0.0983	.6786+/-0.0713
4		.3972+/-0.0655	.6026+/-0.0968	.5808+/-0.1542	.5564+/-0.0495	.5869+/-0.0781	.6653+/-0.0339	.6980+/-0.0639
5		.4064+/-0.0897	.6335+/-0.0371	.5942+/-0.0459	.5269+/-0.1264	.6696+/-0.0371	.6212+/-0.0491	.7092+/-0.0468
6		.6173+/-0.0361	.5160+/-0.0676	.6325+/-0.0542	.6549+/-0.0402	.8011+/-0.0658	.5623+/-0.0975	.7000+/-0.0650
7		.4767+/-0.0638	.6546+/-0.0678	.6785+/-0.0395	.6225+/-0.0819	.6566+/-0.0314	.5864+/-0.0919	.6736+/-0.0316
8		.5560+/-0.0563	.6067+/-0.0927	.6828+/-0.0616	.6932+/-0.0645	.6429+/-0.0722	.6256+/-0.0626	.6477+/-0.0804

'-e'-elbow classification; '-f' -finger classification; '-s'- shoulder classification

VI. CONCLUSION

This work addresses the ability to differentiate the EEG signal to its corresponding left-right movement and elbow-finger-shoulder movement. Wavelet transform and power spectral density estimate are techniques followed in this study for feature extraction. The results presented in this paper indicates that elbow-finger-shoulder movement can be successfully classified using the given set of features, and further this opens up newer avenue for classifications based on composite decision. Experimental results showed that kernelized SVM (RBF-based) showed a superior classification result for multi-class classification.

In light of our present findings, our approach for future work involves the improvement of the accuracy of the classifiers. Also the combination of feature vector is a vital step for proper classification, thus newer features are needed to be tried out which would be simple, robust and require less computational time with higher accuracy, which would be more apt to control EEG based BCI devices. Future study in this direction will aim at techniques for optimizing feature selection, extraction and classification methodologies to be implemented in online classification of EEG data for BCI research.

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