

A non-destructive method to calibrate the torsional spring constant of atomic force microscope cantilevers in viscous environments

Clodomiro Cafolla^{1*}, Amir F. Payam^{2*}, and Kislon Voitchovsky^{1†}

1. Durham University, Physics Department, Durham DH1 3LE, UK
2. University of Bristol, Faculty of Engineering, Bristol BS8 1TH, UK.

* These authors contributed equally to this work

† Corresponding author: kislon.voitchovsky@durham.ac.uk

Abstract

Calibration of the torsional spring constant of atomic force microscopy cantilevers is fundamental to a range of applications, from nanoscale friction and lubrication measurements to the characterization of micro-electromechanical systems and the response of biomolecules to external stimuli. Existing calibration methods are either time consuming and destructive (*ex situ* static approaches), or rely on models using the frequency and quality factor (Q-factor) of the cantilever torsional resonance as input parameters (*in situ* dynamical approaches). While *in situ* approaches are usually preferred for their easy implementation and preservation of the cantilever, their dependence on the torsional resonance Q-factor renders calibration in highly viscous environments challenging. This is problematic, for example, in many nanoscale tribological applications. Here, we propose a calibration method that does not depend on the cantilever torsional Q-factor, and show how the cantilever deflection can be converted into a lateral force. The method is tested with six cantilevers of different shapes and material composition, and in six fluid media. The derived spring constants are compared with predictions from existing methods, demonstrating a higher precision, in particular for highly viscous liquids.

Introduction

Atomic force microscopy (AFM) is a widely used tool for surface characterization, allowing both imaging at nanometer scales and measuring forces in the nano- to piconewton range¹⁻³. While the most common AFM operation relies on measuring the flexural bending of a rectangular cantilever^{4,5} that quantifies forces normal to a sample, torsional measurements are becoming increasingly popular for their ability to extract in-plane forces such as the frictional force with nanoscale lateral precisions⁶⁻⁸. In torsional measurement, the sample is moved laterally with respect to the main axis of the cantilever, making the cantilever twisting as the AFM tip rubs against the sample's surface. The shear force between the tip and the sample can be accurately determined from the twisting angle of the cantilever, provided that the torsional spring constant and the inverse optical lever sensitivity (InvOLS) of the system are known. The InvOLS is a constant depending on the geometry of the system, and allows conversion of the raw photodiode measurement, taken in volts, into nanometer of lateral torsion at the tip.

While the flexural calibration of cantilever is relatively straightforward (see e.g. comprehensive reviews^{9,10}), the torsional calibration is usually more complex and often cannot be achieved *in situ*, or without specialist, homebuilt equipment¹¹⁻¹³. Methods for the calibration of torsional forces, can be broadly classified into three main categories¹⁴: (i) theoretical¹⁵⁻¹⁷, (ii) static^{12,18,27-31,19-26} and (ii) dynamic^{14,32,33}. Theoretical methods typically calculate the spring constant analytically from parameters characterizing the cantilever's geometry and its mechanical properties¹⁵⁻¹⁷. Such methods are particularly sensitive to errors originating from manufacturing variations in cantilevers' dimensions and material properties. Static methods, in contrast, offer a direct measure of the lateral spring constant. These rely on a well-defined lateral force or displacement being applied to the AFM tip which generates torsional bending, thereby allowing the calculation of the torsional spring constant^{12,18-20}. While static methods do not require many assumptions about cantilever's geometry or material properties, they often require extra equipment and hard mechanical contact with a sample surface, leading to tip damage. These techniques are hence considered *ex situ* and hence more time consuming. Finally, dynamic calibration methods usually rely on the torsional resonance frequency of the cantilever to find its spring constant^{11,32,33}.

Arguably, the best known torsional dynamic calibration methods are the so-called Cleveland method³² and Sader method³²⁻³⁴. The Cleveland method measures the

torsional frequency changes of the cantilever induced by the on-axis loading of added masses in order to deduce its torsional spring constant. In contrast, the Sader method determines the cantilever's torsional spring constant from its interaction with the surrounding medium, as quantified by the cantilever hydrodynamic function. The Sader method is particularly straightforward because it only requires the frequency and associated quality factor (Q-factor) of the cantilever torsional resonance as input parameters. As a result, the Sader method has become one of the most popular approaches in the scientific community to calibrate microcantilevers. While highly successful in most common conditions, the dependence of the Sader method on the cantilever's hydrodynamic function can become problematic in viscous environments. Practically, this comes from the need to know the Q-factor of the cantilever, a quantity difficult to measure accurately in highly viscous liquids where the resonance can significantly broaden in the frequency domain. Additionally, the method assumes a Q-factor significantly larger than unity. This assumption, although commonly verified in air, tends to fail in liquids, especially for those with higher viscosity³³. As a result, the calculated torsional spring constant can vary significantly when derived in different viscous media, despite being an intrinsic property of the cantilever³³. An alternative method that does not rely on the Q-factor is hence highly desirable.

Here, we propose an alternative torsional calibration method that requires knowledge of three easily accessible parameters: the fundamental torsional resonance frequencies of a cantilever in air and in the medium of interest, and the cantilever length and width. Significantly, the method is independent of the cantilever Q-factor, non-destructive and can be carried out on commercial AFMs without any further modifications. Since in most cases, the spring constant is only useful if the InvOLS is known, we adapt an existing InvOLS calibration methodology described elsewhere (ref.³³) to also derive the system's InvOLS. The InvOLS calculation is based on the same three aforementioned parameters, on the Q-factor and on the power spectrum density of the cantilever torsional motion at DC (P_{DC}), obtained from the cantilever's thermal torsional vibration spectrum. This allows for a more accurate value of the InvOLS because the quantity now depends on the inverse of the square root of the Q-factor, as opposed to the inverse of the Q-factor with the Sader formula. To validate our approach, we compare results derived with our method and the Sader method using different cantilevers in different media.

Experimental

The experimental section firstly derives expressions for the cantilever's torsional spring constant and InvOLS based on suitable observables. Secondly, all the details about the materials and methods of the experimental measurements are presented.

Theory

Let's consider a cantilever of length L , width b and thickness h . Assuming that L is much greater than b and h , the torsional spring torque at the cantilever end is given by:³²

$$k_\phi = \frac{1}{3\pi^2} \rho_c h b^3 L \omega_{t,a}^2, \quad (1)$$

where ρ_c is the cantilever density and $\omega_{t,a}$ is the torsional resonance frequency of cantilever in air. While it is possible to directly use Eq. (1) to calculate the torsional spring constant of the cantilever, there are in practice several important limitations. First, Eq. (1) requires knowledge of the cantilever thickness, a parameter that often carries a large variability with respect to the nominal value (see Fig. S1 in the SI for a representative example). Second, this equation relies on the assumption of the cantilever's density being homogenous. This is not always valid, with local inhomogeneities potentially affecting both the geometry and density of the cantilever. We hence use the areal mass density in order to derive an effective cantilever density. We assume, then, that the cantilever dynamics in a dense fluid can be described by a simplified hydrodynamic function of torsional motion, $\Gamma_{\text{tors}}(\omega)$ characterized by two real (a_1, a_2) and one imaginary (b_1) regression coefficients as^{35,36}:

$$\Gamma_{\text{tors}}(\omega) \sim \left(a_1 + \frac{a_2}{\sqrt{Re}} \right) + j \left(\frac{b_1}{\sqrt{Re}} \right). \quad (2)$$

a_1, a_2 and b_1 are the regression coefficients of the hydrodynamic function for the torsional motion of a rectangular cantilever in fluid environments. The values of a_1, a_2 and b_1 are 0.0634, 0.388 and 0.4, respectively^{35,36}. Here, the fluid parameters are encapsulated by the Reynold's number, $Re = \rho_l \omega b^2 / 4\eta$, where ρ_l and η are the fluid density and viscosity, respectively. Using Eq. (2), we can relate the torsional resonance

frequency of the cantilever in air, $\omega_{t,an}$, with that in liquid, $\omega_{t,fn}$, for any given vibration eigenmode, n .^{32,37}

$$\omega_{t,fn}^2 \left[\frac{3\pi a_1 \rho_f b}{2\rho_c h} + 1 \right] + \omega_{t,fn}^{\frac{3}{2}} \left[\frac{6\pi a_2 \sqrt{\eta} \sqrt{\rho_f}}{2\rho_c h} \right] = \omega_{t,an}^2. \quad (3)$$

Using Eq. (3), the areal mass density of cantilever $\rho_c h$ can be calculated as follows:

$$\widehat{\rho h} = \frac{3\omega_{t,f1}^2 \pi a_1 \rho_f b + 6\pi a_2 \sqrt{\omega_{t,f1}^3 \rho_f \eta}}{2(\omega_{t,a1}^2 - \omega_{t,f1}^2)}. \quad (4)$$

Equation (4) can be used along with Eq. (1) to acquire the torsional torque constant (in Newton per radian) of the cantilever:

$$k_\phi = \frac{3\omega_{t,f1}^2 \pi a_1 \rho_f b^4 + 6\pi a_2 b^3 \sqrt{\omega_{t,f1}^3 \rho_f \eta}}{6\pi^2 (\omega_{t,a1}^2 - \omega_{t,f1}^2)} L \omega_{t,a1}^2, \quad (5)$$

which only requires the beam width and the torsional resonance frequencies in air and liquid as input parameters, alongside the density and viscosity of the fluid. The torsional spring constant (in N/m) of the cantilever can then be obtained from the torsional torque constant using the following equation³³:

$$k_t = \frac{k_\phi L}{(L - \Delta L) h_t^2}, \quad (6)$$

where ΔL is the distance between the position of the tip and the end of cantilever, and h_t is the tip height.

The spring constant can be used alongside the torsional InvOLS, γ , as formulated in ref.³³, so as to multiply the cantilever deflection in volts and obtain the lateral force:

$$\gamma = h \sqrt{\frac{2k_B T}{\pi k_\phi f_o P_{DC} Q}}, \quad (7)$$

where P_{DC} is the power spectrum density of the cantilever torsional motion at DC, measured on the cantilever's thermal torsional vibration spectrum, k_B is the Boltzmann's constant and T is the temperature.

Materials and Methods

The frequency response of six commercially available cantilevers was investigated, each in six different media. The cantilevers are OMCL-RC800PSA (4 different cantilever on a same chip, Olympus, Tokyo, Japan), AD-2.8AS (Adama Innovations LTD, Dublin, Ireland), and HQ-NSC18/HARD AL-BS (Windsor Scientific, Slough, UK). For clarity, the nominal geometrical and physical characteristics of the different cantilevers (hereafter referred to as C1–C6) are summarized in Table 1.

Fig. 1(a) highlights the different geometrical characteristics of the cantilevers used: C1–4 have a rectangular shape; C5 and C6 are a combination of a rectangle at the chip end and a triangle at the tip end.

Cantilever	Commercial Name	Length (μm)	Width (μm)	Tip Height (μm)	Material
C1	OMCL-RC800PSA	100.0	20.0	2.9	Silicon Nitride
C2	OMCL-RC800PSA	100.0	40.0	2.9	Silicon Nitride
C3	OMCL-RC800PSA	200.0	20.0	2.9	Silicon Nitride
C4	OMCL-RC800PSA	200.0	40.0	2.9	Silicon Nitride
C5	AD-2.8-AS	225.0	35.0	12.5	Diamond
C6	HQ-NSC18/HARD AL-BS	225.0	27.5	15.0	Diamond-like carbon

Table 1. Summary of the characteristics of the cantilevers (C1–C6) used for this study.

As measurement media, we used air, ultrapure water, isopropanol, methanol, dimethyl sulfoxide (DMSO), hexadecane and squalane. The ultrapure water (AnalaR Normapur) was purchased from VWR International Ltd (Lutterworth, UK). All the other chemicals were purchased from Sigma-Aldrich (Dorset, UK) with a purity $> 99\%$ and used without any further purification. The tabulated density and viscosity of each fluid at the experimental temperature in Table 2:

Medium	Density (kg/m ³)	Viscosity (Pa s)
Air	1.18	1.83×10^{-5}
Methanol	787.00	5.43×10^{-4}
Water	998.00	8.90×10^{-4}
DMSO	1095.00	1.99×10^{-3}
Isopropanol	785.00	2.10×10^{-3}
Hexadecane	769.00	3.08×10^{-3}
Squalane	805.00	2.80×10^{-2}

Table 2. Density and viscosity values for all the media³⁸⁻⁴⁰ at 25 °C.

The measurements were conducted on a commercial Cypher ES AFM (Asylum Research, Santa Barbara, CA) equipped with a temperature-controlled sample stage. For each medium and for each cantilever, thermal spectra were recorded at 25°C. To minimize any errors associated with changes in the laser alignment in different fluids, all the media were explored in a same session for each cantilever. When exchanging fluids within a given series, the tip was thoroughly washed with isopropanol (20 times with 100 μ l) and then with the new solution of interest (40 times with 100 μ l).

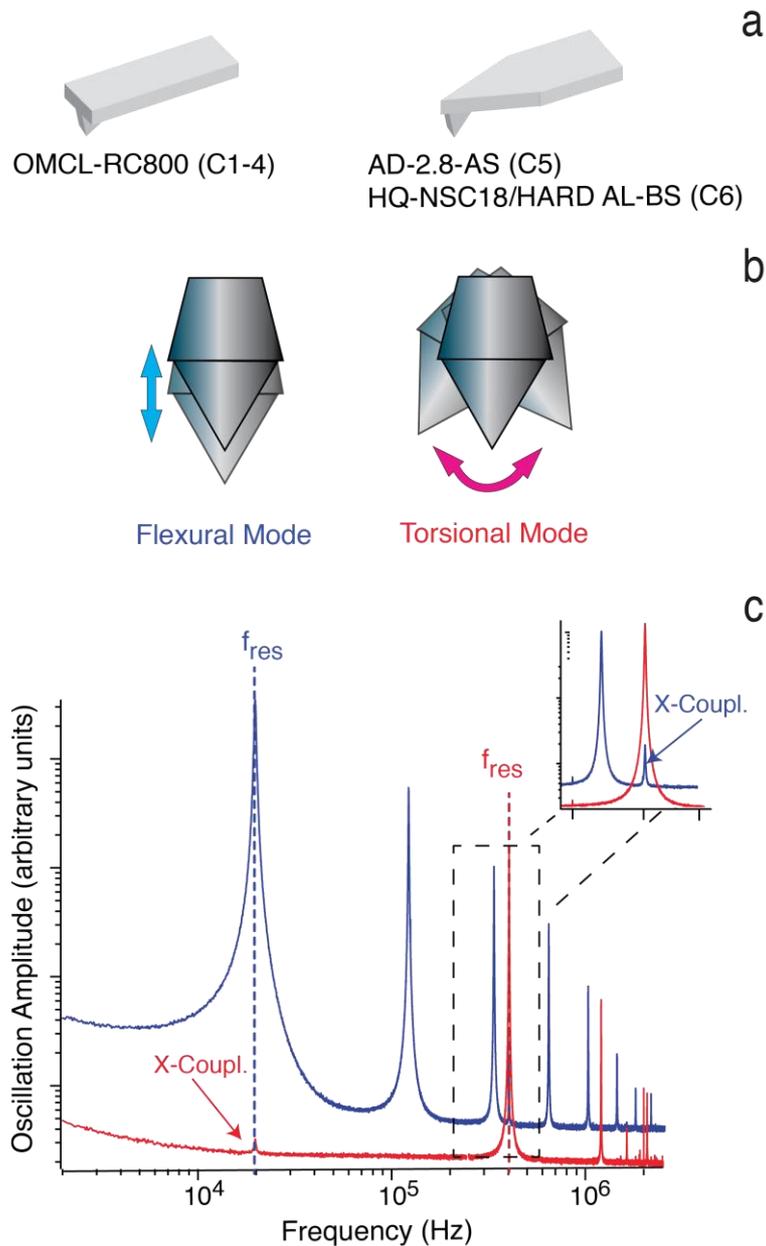


Fig. 1. Cantilever types and calibration details for flexural vs torsional modes. (a) Geometry of the cantilevers used in the study. (b) Pictorial representation of the different motion of the cantilever in flexural and torsional mode. (c) Representative example of flexural (blue) and torsional (red) thermal spectra for a given cantilever. In each case, the resonance frequency, f_{res} , of the first eigenmode is shown. Cross-coupling occurs between the two modes is negligible for our purposes.

The frequency response of the cantilevers in the different media was investigated by recording the thermal spectrum of each cantilever in each medium. The Brownian motion of the fluid surrounding the cantilever results in naturally exciting the cantilever itself and determining a flexural and a torsional motion. The two different types of motion can be selectively detected using the AFM laser. Fig. 1(b) schematically shows

the different dynamics between flexural and torsional motion of the cantilever. The two motions result in different thermal spectra, as shown in Fig. 1(c). Tables S1-6 in the Supplementary Information provide a detailed summary of the frequency responses of the cantilevers in the different media.

Results and discussion

Figure 2 compares the new method proposed here with the Sader method. Representative results are given for the spring constant of cantilever C3 in all the six fluids.

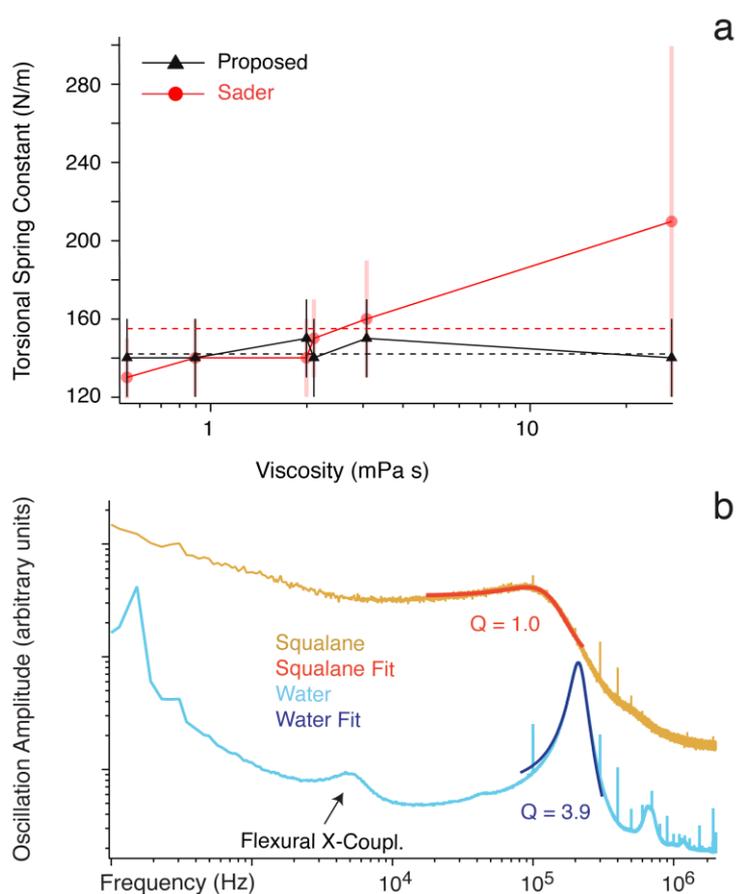


Fig. 2. (a) Comparison of predictions derived with the proposed method and the Sader method in fluids of varying viscosity for cantilever C3 used as an example. The dashed lines represent the average spring constant for each method. The proposed method appears more precise considering its smaller deviation from the mean value. Predictions from the Sader method are significantly more dependent on viscosity variations between media. See supplementary Figs. S2-S6 for the results obtained with the other cantilevers. (b) Representative thermal spectra in low and high viscosity media (water and squalane, respectively). In both cases, the first eigenmode is fitted

with the thermal noise mode^{4,5,33,41-44} In high viscosity media, the Q-factor significantly decreases and approaches unity, rendering the fitting procedure prone to large variations in the derived Q value depending on the fitting interval. Error bars in (a) are calculated using standard formulae for error propagation (see Supplementary Information, section 3). The data points and error bars relative to the Sader method have been shadowed and enlarged so as to enhance graph readability. The thermal spectrum of squalane in (b) has been offset vertically for clarity.

For all the cantilevers studied we found our method to be significantly less sensitive to viscosity in determining the spring constant. The robustness of our approach is particularly obvious in highly viscous media (Fig. 2a) where the dependence of the Sader method on the cantilever Q-factor hinders predictions. Accurate determination of the Q-factor is strongly dependent on the fitting interval selected in the thermal spectrum, especially since Q may be close to unity³³ (Fig. 2b). In the case of C2 and C6 (see Supplementary Information, Fig. S2 and S5), our method appears more robust than the Sader method also in low viscous media. This is not surprising since the Sader method relies on the assumption of a Q-factor much greater than unity, a condition which is typically met for stiff cantilevers in air^{32,33,44}. However, applying the method can be challenging even in media with viscosity as low as water³³.

As illustrated in Figs. 2(a), S2-6 and in Tables S1-6, the proposed approach shows also greater precision in comparison the Sader method: for highly viscous media, the error is significantly smaller and, in some cases, reduced up to four times. For cantilevers C5-6 (Figs. S5-6 and Tables S5-S6), the uncertainty is smaller in all the media considered. In order to quantitatively assess the robustness of our method, we calculated the relative variability of predictions for each cantilever across the different media (Fig. 3). Here, the relative variability is defined as the difference between the maximum and the minimum spring constant normalized by the average value.

The results clearly confirm the robustness of our method against the impact of the surrounding fluid's viscosity with the normalized variability range being, in some cases, even more than 4 times smaller with the proposed method. In Fig. 3(b) we consider a reduced set excluding the highest viscosity data point (squalane) given its possible biasing of the results. Again, our method remains significantly less sensitive to viscosity changes in comparison with the Sader method. Further statistical data analysis on the spring constant variability is available in the Supplementary Information (Fig. S7).

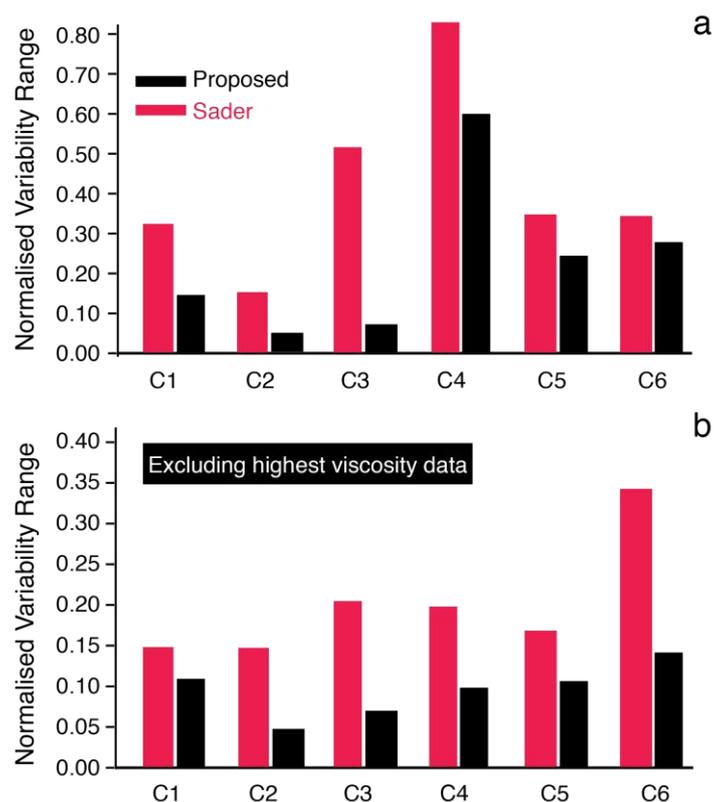


Fig. 3. Quantification of the variability across media for each cantilever's torsional spring constant for the proposed and Sader methods. In (a) the variability is calculated using the data in all the media, whereas in (b) we have excluded the data relative to the highest viscosity medium (squalane). For each cantilever, the variability of the spring constant across media is calculated as the difference between the maximum and the minimum spring constant normalized by the average value.

Our method could, in principle, be extended to the calibration of arbitrarily shaped cantilevers, but this would require prior determination of an effective cantilever width from a torsional perspective. This task is non-trivial task with, to the best of our knowledge, no simple existing approach for calculating the effective width. Attempts to calibrate the torsional spring constant of a triangular cantilever confirmed that our method tends to be more robust against the influence of viscosity variability, but the values derived are partly speculative for lack of reliable input (effective width) and the absence of independent comparative measurements (see section 5 of the Supplementary Information).

Combining equations 5 and 7, it is possible to calculate easily the torsional InvOLS of the cantilevers, hence allowing a straightforward derivation of the lateral shear force

experienced by the AFM tip. Our method would hence also potentially increase the accuracy of the torsional InvOLS calculation. This is because in our method the torsional InvOLS depends on the inverse of the square root of the Q-factor, whereas in currently used models there is a linear dependence of the InvOLS on the inverse of the Q-factor³³. We note that our method relies on knowledge of P_{DC} from the thermal spectrum of the cantilever. While the value of P_{DC} can be readily obtained in most commercial AFMs, it is worth mentioning that additional gains and filters are often applied to the lateral deflection signal by commercial software in default settings. This may lead to an unexpectedly high or low InvOLS due to the P_{DC} value being incorrect.

Conclusions

In this paper, we present a non-destructive and non-invasive method to determine the torsional spring constant of a cantilever, and to calculate the lateral shear force experienced by the AFM tip from the raw deflection as obtained from the photodetector. The method requires only on three input parameters: the fundamental torsional resonance frequencies of the cantilever in air and in the medium of interest, and the cantilever width. Significantly, the method is independent from the cantilever Q-factor which renders our method particularly effective in high viscosity media. We validate our approach with cantilevers exhibiting different geometries and in six different media. Our method can be carried out on commercial AFMs without the need for any extra equipment. We believe that proposed method could be particularly useful for quantitative high-resolution torsional imaging in solution⁴⁶, and in the field of nanoscale friction and tribology, for example when investigating ionic liquids⁴⁷, organic lubricants⁶, surfactants layers⁴⁸ and functional nano-interfaces⁴⁹. In order to facilitate the use of our method, the script of a Python code capable of calculating the torsional spring constant, its uncertainty, and the torsional amplitude InvOLS using the proposed method is given in the last section of the Supplementary Information.

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References

- 1 J. M. Fernandez and H. Li, *Science* 303, 1674 (2004).
- 2 M. Grandbois, M. Beyer, M. Rief, H. Clausen-Schaumann and H. E. Gaub, *Science* 283, 1727 (1999).
- 3 R. García, R. Magerle and R. Perez, *Nat. Mater.* 6, 405 (2007).
- 4 M. J. Higgins, R. Proksch, J. E. Sader, M. Polcik, S. Mc Endoo, J. P. Cleveland and S. P. Jarvis, *Rev. Sci. Instrum.* 77, 013701 (2006)
- 5 J. E. Sader, J. W. M. Chon and P. Mulvaney, *Rev. Sci. Instrum.* 70, 3967 (1999).
- 6 K. Voitchovsky, *Nanoscale* 8, 17472 (2016)
- 7 T.D. Li and E. Riedo, *Phys. Rev. Lett.* 100, 106102 (2008).
- 8 C. Cafolla and K. Voitchovsky, *Nanoscale*, (2018).
- 9 C. T. Gibson, A. Smith and C. J. Roberts, *Nanotechnology* 16, 234 (2005).
- 10 M. L. B. Palacio and B. Bhushan, *Crit. Rev. Solid State Mater. Sci.* 35, 73 (2010).
- 11 M. Munz, *J. Phys. D* 43, 063001 (2010).
- 12 R. J. Cannara, M. Eglin and R. W. Carpick, *Rev. Sci. Instrum.* 77, 053701 (2006).
- 13 K.-H. Chung, J. R. Pratt and M. G. Reitsma, *Langmuir* 26, 1386 (2010).
- 14 J. D. Parkin and G. Hähner, *Nanotechnology* 25, 225701 (2014).
- 15 R. Álvarez-Asencio, E. Thormann and M. W. Rutland, *Rev. Sci. Instrum.* 84, 096102 (2013).
- 16 J. M. Neumeister and W. A. Ducker, *Rev. Sci. Instrum.* 65, 2527 (1994).
- 17 J. L. Hazel and V. V. Tsukruk, *J. Tribol.* 120, 814 (1998).
- 18 M. G. Reitsma, R. S. Gates, L. H. Friedman and R. F. Cook, *Rev. Sci. Instrum.*, 82, 093706 (2011).
- 19 E. Liu, B. Blanpain and J. P. Celis, *Wear* 192, 141 (1996).
- 20 E. Tocha, J. Song, H. Schönherr and G. J. Vancso, *Langmuir* 23, 7078 (2007).
- 21 A. Feiler, P. Attard and I. Larson, *Rev. Sci. Instrum.* 71, 2746 (2000).
- 22 G. Bogdanovic, A. Meurk and M. W. Rutland, *Colloids Surf. B* 19, 397 (2000).
- 23 H. Xie, J. Vitard, S. Haliyo and S. Régnier, *Rev. Sci. Instrum.* 79, 096101 (2008).
- 24 M. G. Reitsma, *Rev. Sci. Instrum.* 78, 106102 (2007).
- 25 D. F. Ogletree, R. W. Carpick and M. Salmeron, *Rev. Sci. Instrum.* 67, 3298 (1996).
- 26 D. Choi, W. Hwang and E. Yoon, *J. Microsc.* 228, 190 (2007).
- 27 M. Varenberg, I. Etsion and G. Halperin, *Rev. Sci. Instrum.* 74, 3362 (2003).
- 28 X. Ling, H.-J. Butt and M. Kappl, *Langmuir* 23, 8392 (2007).
- 29 D. B. Asay and S. H. Kim, *Rev. Sci. Instrum.* 77, 043903 (2006).
- 30 S. Ecke, R. Raiteri, E. Bonaccorso, C. Reiner, H.-J. Deiseroth and H.-J. Butt, *Rev. Sci. Instrum.* 72, 4164 (2001).
- 31 R. G. Cain, M. G. Reitsma, S. Biggs and N. W. Page, *Rev. Sci. Instrum.* 72, 3304 (2001).
- 32 C. P. Green, H. Lioe, J. P. Cleveland, R. Proksch, P. Mulvaney and J. E. Sader, *Rev.*

- Sci. Instrum. 75, 1988 (2004).
- 33 N. Mullin and J. K. Hobbs, Rev. Sci. Instrum. 85, 113703 (2014).
- 34 C. P. Green and J. E. Sader, J. Appl. Phys. 92, 6262 (2002).
- 35 T. Cai, ProQuest Dissertations Publishing 3601316, 1 (2013).
- 36 T. Cai, F. Josse, S. Heinrich, N. Nigro, I. Dufour and O. Brand, FCS 2012 IEEE International, 1 (2012)
- 37 C. A. Van Eysden and J. E. Sader, J. Appl. Phys. 100, 114916 (2006).
- 38 J. Kestin, M. Sokolov and W. A. Wakeham, J. Phys. Chem. Ref. Data 7, 941 (1978).
- 39 H. D. Young and R. A. Freedman, University physics with modern physics, (2012).
- 40 Tables: Anton Paar Wiki, <https://wiki.anton-paar.com/en/tables/>, (accessed 22 June 2018).
- 41 J. L. Hutter and J. Bechhoefer, Rev. Sci. Instrum. 64, 1868 (1993).
- 42 H.-J. Butt and M. Jaschke, Nanotechnology 6, 1 (1995).
- 43 S. M. Cook, K. M. Lang, K. M. Chynoweth, M. Wigton, R. W. Simmonds and T. E. Schäffer, Nanotechnology 17, 2135 (2006)
- 44 T. Pirzer and T. Hugel, Rev. Sci. Instrum. 80, 035110 (2009).
- 45 C. E. Brown, Applied Multivariate Statistics in Geohydrology and Related Sciences, 155 (1998).
- 46 N. Mullin and J. K. Hobbs, Phys. Rev. Lett. 107 (2011).
- 47 F. Endres, N. Borisenko, S. Z. El Abedin, R. Hayes, R. Atkin, Faraday Discuss. 154, (2012).
- 48 R. Atkin and G. G. Warr, JACS 127, (2005).
- 49 K. Voitchovsky, D. Giofre, J. J. Segura, F. Stellacci and M. Ceriotti, Nat Commun. 7, (2016).